



**SAPIENZA**  
UNIVERSITÀ DI ROMA

**Nano** Rome, 20-23 September  
**2016 Innovation**  
Conference & Exhibition

# The Role of Electronic Excitations in Solution-Processed Oligothiophene Small-Molecules for Organic Solar Cells from First Principles.



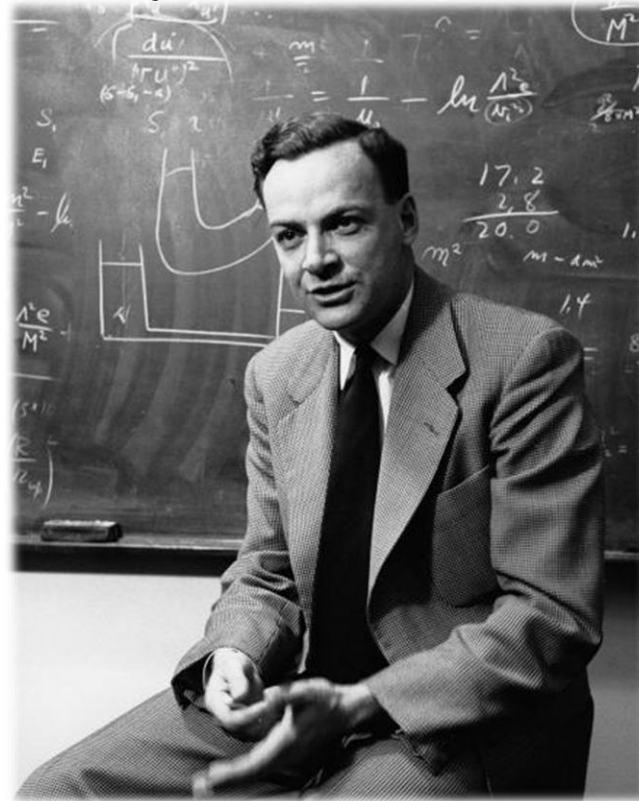
**Dr. Fabrizio Gala**

**Dipartimento di Scienze di Base e Applicate  
Per l'Ingegneria (SBAI)**



**SAPIENZA**  
**UNIVERSITÀ DI ROMA**

**R.P. Feynman**



**Nano** Rome, 20-23 September  
**2016 Innovation**  
Conference & Exhibition

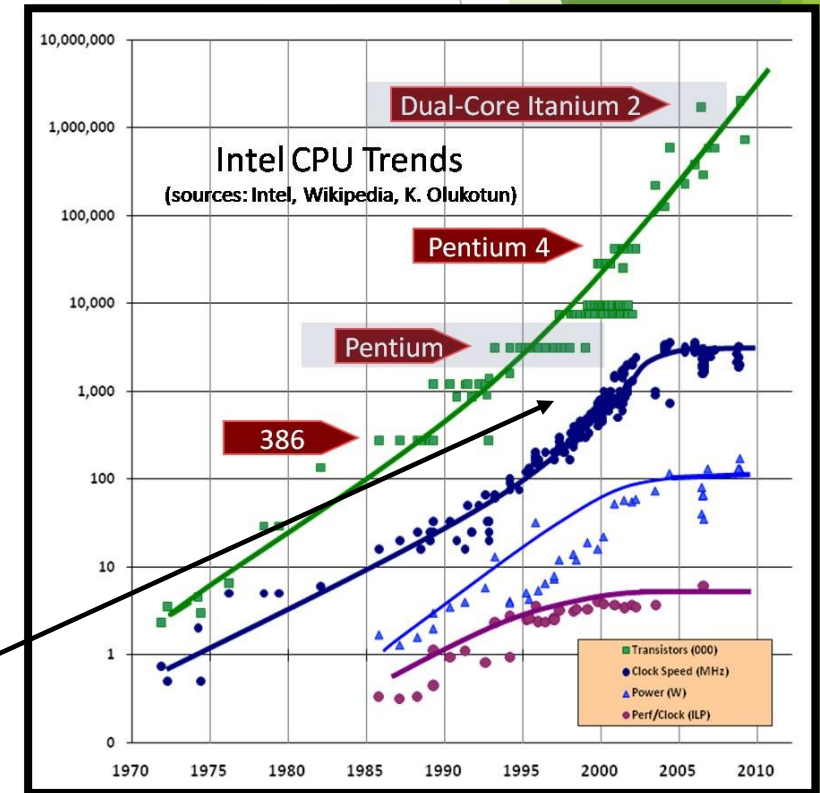
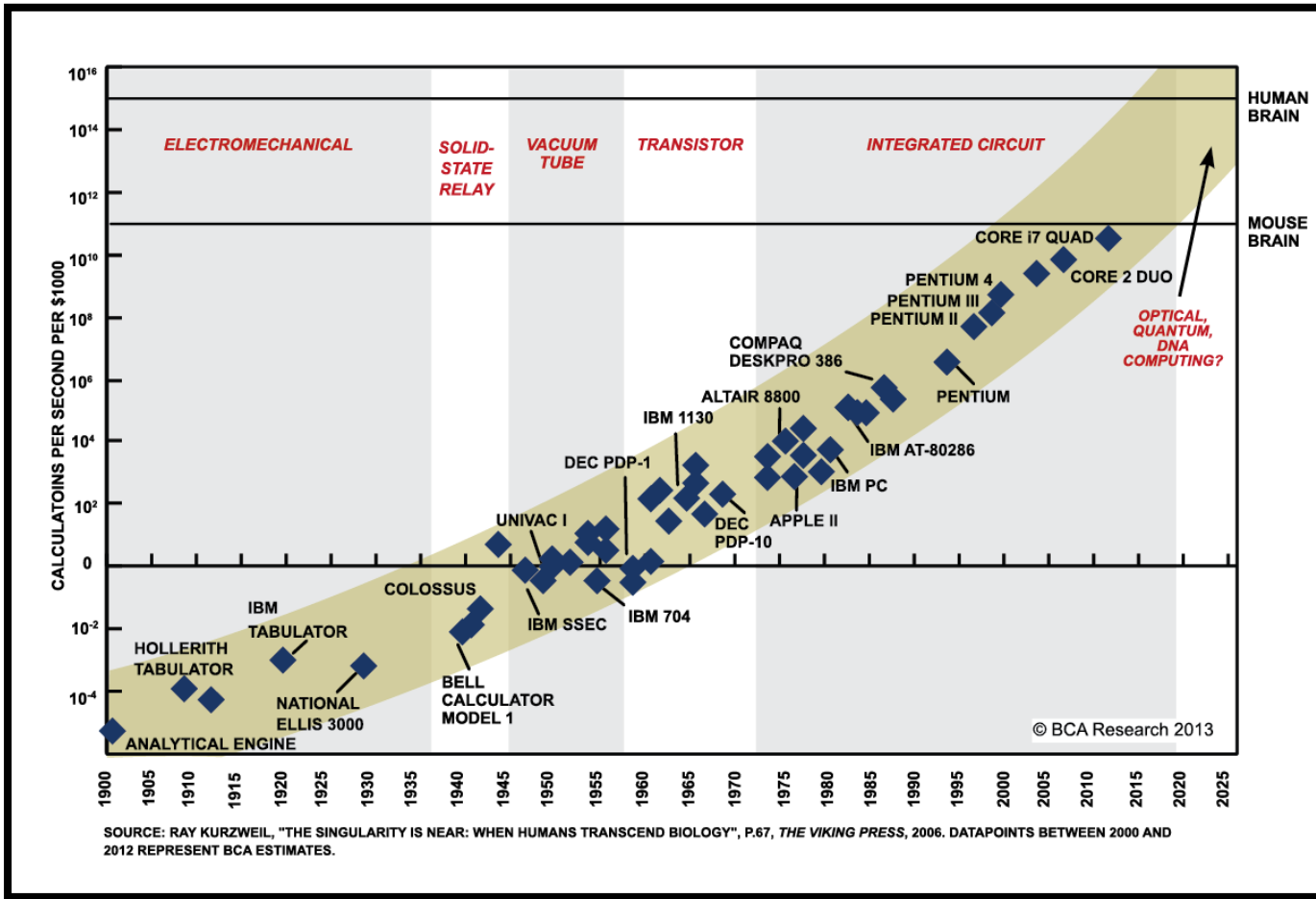
*«Nature isn't classical, dammit, and if you want to make a simulation of nature, you'd better make it quantum mechanical, and by golly it's a wonderful problem, because it doesn't look so easy.»*

from "Simulating Physics with Computers",  
International Journal of Theoretical Physics, volume 21, 1982, p. 467-488



# What about Computing Power ?

Moore's law:  $y \propto 2^{\frac{2}{3}x}$



Moore's law keeps going, defying expectations  
(thanks mainly to transistor size miniaturization)



TOP500 - Wikipedia - Mozilla Firefox

https://it.wikipedia.org/wiki/TOP500#cite\_note-4

server DAAP with itunes 10

quello esistente nel novembre del 1993, il Connection Machine CM-5/1024 (con 1024 core ed un peak di 151 GFLOPS).

Lista (prime 10 posizioni) [ modifica | modifica wikitesto ]

La seguente tabella mostra le prime dieci posizioni della 44ª TOP500, pubblicata nel novembre 2014<sup>[3]</sup>

Posizione	Rmax Rpeak (TFLOPS)	Nome	Computer Core, Architettura	Produttore	Sito Nazione, Anno	Sistema operativo
1	33.863 54.902	<i>Tianhe-2</i>	<b>NUDT</b> Xeon E5-2692 + Xeon Phi 3151P, TH Express-2	NUDT	National Supercomputing Center in Guangzhou Cina, 2013	Linux
2	17.590 27.113	<i>Titan</i>	<b>Cray XK7</b> Opteron 6274 + Tesla K20X, Cray Gemini Interconnect	Cray Inc.	Oak Ridge National Laboratory Stati Uniti, 2012	Linux
3	17.173 20.133	<i>Sequoia</i>	<b>Blue Gene/Q</b> PowerPC A2, Custom	IBM	Lawrence Livermore National Laboratory Stati Uniti, 2013	Linux
4	10.510 11.280	<i>K computer</i>	<b>RIKEN</b> SPARC64 VIIIfx, Tofu	Fujitsu	RIKEN Giappone, 2011	Linux
5	8.586 10.066	<i>Mira</i>	<b>Blue Gene/Q</b> PowerPC A2, Custom	IBM	Argonne National Laboratory Stati Uniti, 2013	Linux
6	6.271 7.779	<i>Piz Daint</i>	<b>Cray XC30</b> Xeon E5-2670 + Tesla K20X, Aries	Cray Inc.	Swiss National Supercomputing Centre Svizzera, 2013	Linux
7	5.168 8.520	<i>Stampede</i>	<b>PowerEdge C8220</b> Xeon E5-2680 + Xeon Phi, Infiniband	Dell	Texas Advanced Computing Center Stati Uniti, 2013	Linux
8	5.008 5.872	<i>JUQUEEN</i>	<b>Blue Gene/Q</b> PowerPC A2, Custom	IBM	Forschungszentrum Jülich Germania, 2013	Linux
9	4.293 5.033	<i>Vulcan</i>	<b>Blue Gene/Q</b> PowerPC A2, Custom	IBM	Lawrence Livermore National Laboratory Stati Uniti, 2013	Linux
10	3.577 6.132		<b>Cray CS</b> Xeon E5-2660v2 10C and Nvidia K40, Infiniband	Cray Inc.	Stati Uniti, 2014	Linux

Lista (supercomputer in Italia) [ modifica | modifica wikitesto ]

La seguente tabella mostra i supercomputer in Italia:

Posizione	Sistema	Core	Rmax TFLOPS	Rpeak TFLOPS	Produttore	Sito	Anno
19	HPC2 - iDataPlex DX360M4, Intel Xeon E5-2680v2 10C 2.8GHz, Infiniband FDR, NVIDIA K20x4	72,000	3,188.0	4,605.0	IBM	ENI <sup>[4]</sup>	Novembre 2015
37	Fermi - BlueGene/Q, Power BQC 16C 1.60GHz, Custom	163,840	1,788.9	2,097.2	IBM	CINECA <sup>[5]</sup>	Novembre 2015
130	GALILEO - IBM NextScale nx360M4, Xeon E5-2630v3 8C 2.4GHz, Infiniband QDR, Intel Xeon Phi 7120P4	50,232	684.3	1,103.1	IBM	CINECA	Novembre 2015
206	HPCC1 - iDataPlex DX360M4, Xeon E5-2670 8C 2.600GHz, Infiniband FDR14	24,000	454.1	499.2	IBM	ENI	Novembre 2015



ENI CRENC  
(Centro Ricerche per le  
Energie Rinnovabili)  
Istituto ENI Donegani  
Novara



Measuring heat of formation for a single molecule is 50 times more expensive than accurate quantum chemistry calculation



# Atomic-scale modelling in the industry

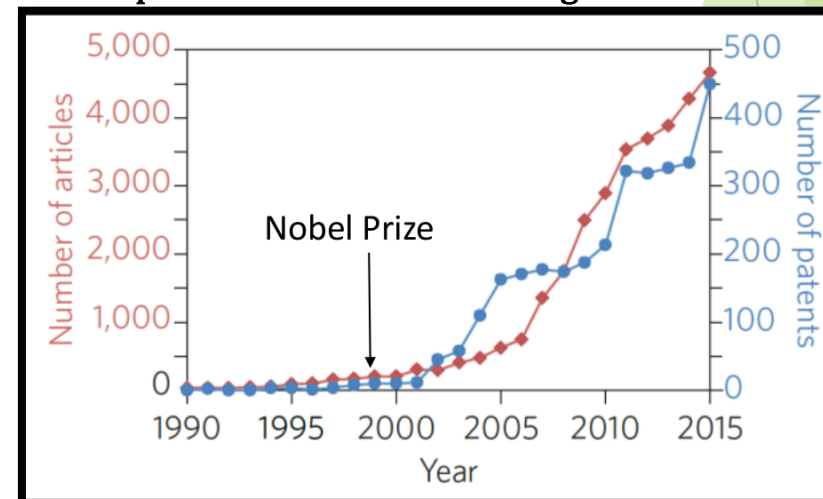
## INDUSTRIAL USERS

- **Chemical** - major chemical companies have modeling groups since the 1980's using discrete models; modelling of solid state systems (heterogeneous catalysis) started later; smaller chemical companies are still in the process of adopting discrete models
- **Electronic** - leading electronics companies have been pioneering discrete models on the electronic and atomistic levels since the 1970's (IBM, NEC, Bell Labs); today major players like Intel, Samsung, Fujitsu, Panasonic, TSMC use commercial software
- **Oil, gas, energy** - leading companies like Shell and ExxonMobil have in-house modelling groups using atomic-scale models; government supported research organizations (IFPEN, Mexian Petroleum Institute) support industrial efforts

Number of articles and patents in materials science including the term "density functional theory" published per year during the past 25 years.

IPC	Description	Percentage
H01	Basic electric elements	~26 %
C07	Organic chemistry	~21%
C ...	Other areas of chemistry	~24 %
B01	Physical or chemical processes	~10 %
A	Health, Medical	~ 6%
G06	Computing, Calculating, Counting	~ 5%

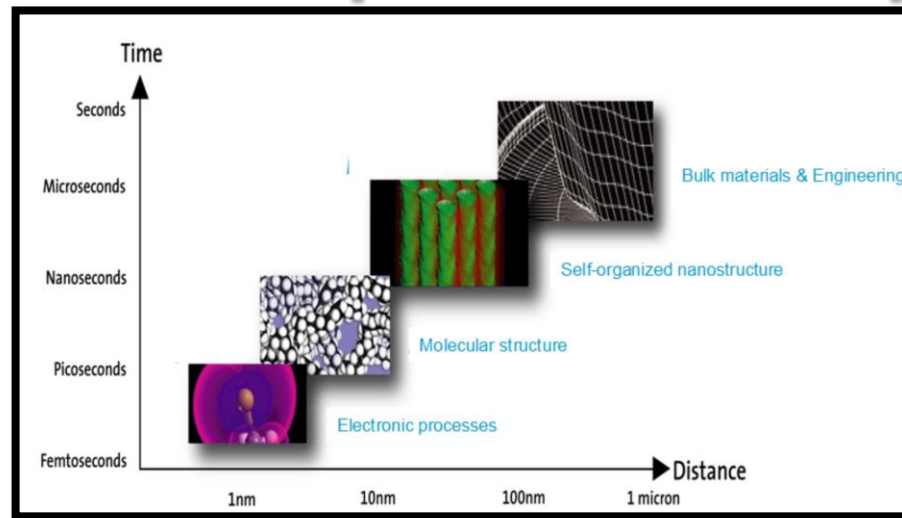
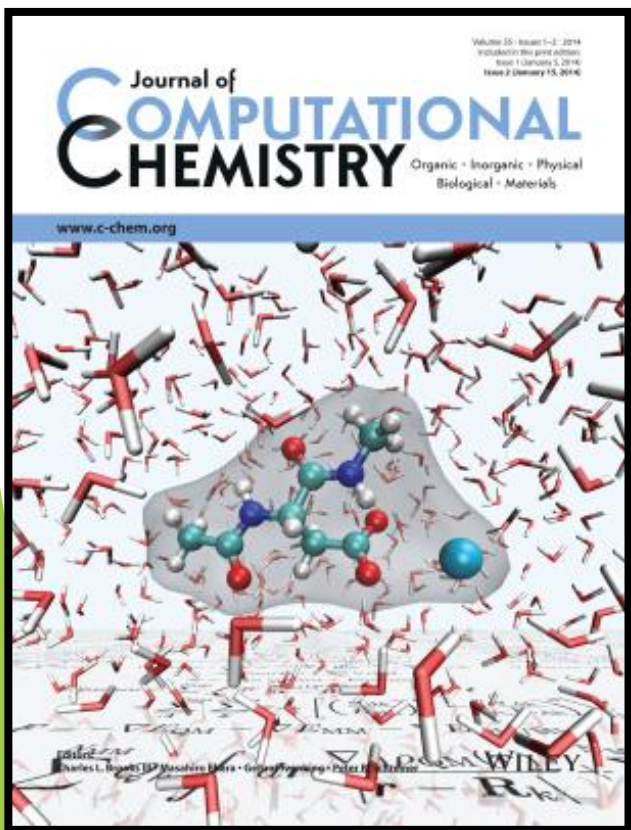
From "the Economic impact of molecular modelling" – Goldbeck Consulting Ltd (2012)





# Multiscale computational approaches

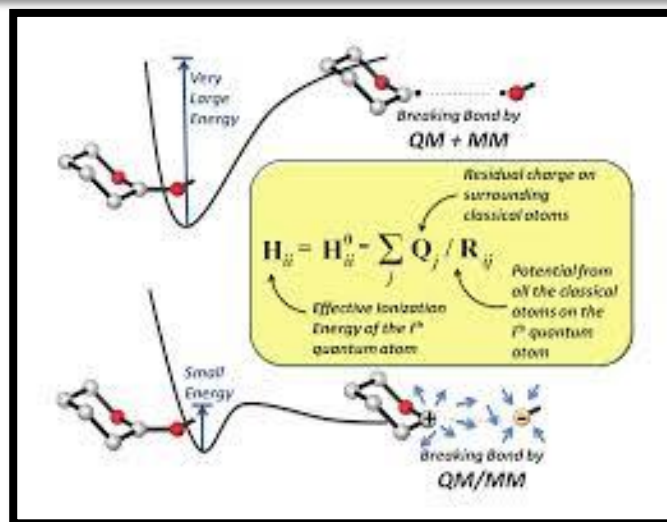
The Nobel Prize in Chemistry 2013 was awarded jointly to M. Karplus, M. Levitt and A. Warshel "for the development of multiscale models for complex chemical systems".



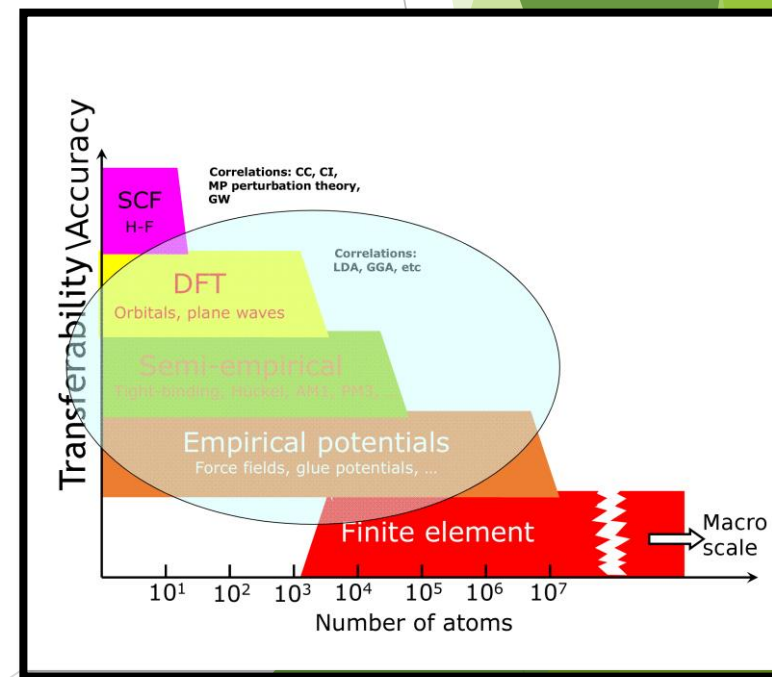
Different length/time scales

Different physical phenomena

Multiscale approach  
(QM/MM for instance)

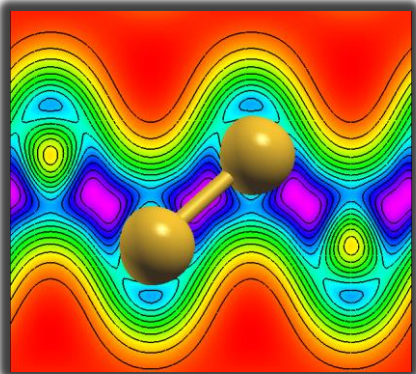


Energetics of C-O breaking in an uncoupled QM + MM (upper diagram) and in a coupled QM/MM (lower diagram)

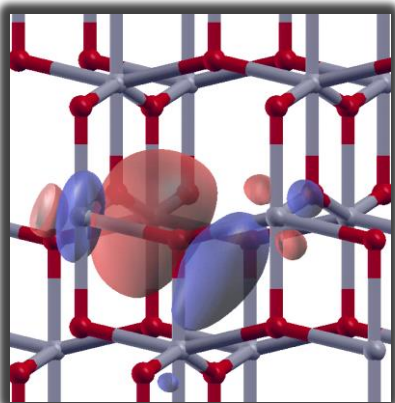




# AB-INITIO CALCULATIONS: Density Functional Theory(1)



Silicon electron charge density in a FCC crystal.



Pseudo sp<sup>2</sup> orbital in TiO<sub>2</sub> anatase bulk phase

The total energy is a functional of the electron density only, then:

- 1) A universal Hohenberg-Kohn Functional  $F_{HK}[n(\mathbf{r})]$  exists
- 2) The external potential corresponds to a given density and viceversa

$$F_{HK}[n_R(\mathbf{r})] = T[n_R(\mathbf{r})] + U_{ee}[n_R(\mathbf{r})]$$

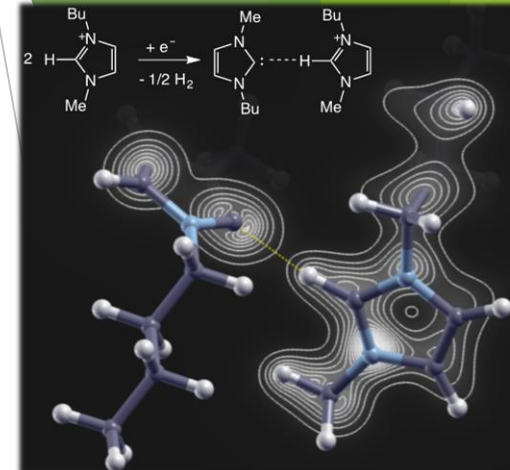
$$E[n_R(\mathbf{r})] = F_{HK}[n_R(\mathbf{r})] + \int V_R^{ext}(\mathbf{r})n_R(\mathbf{r})d^3r$$

Contains all the complicated physical aspects of electron-electron interactions

**ELECTRON DENSITY**

$$n_R(\mathbf{r}) \equiv n(\mathbf{r}) = \sum_k f(\epsilon_k) \|\psi_k(\mathbf{r})\|^2$$

Energy Minimization is carried out by solving (self-consistently) the Khon-Sham (KS) Equations:

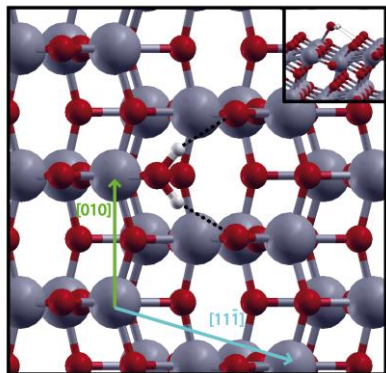
$$\left( -\frac{1}{2} \nabla^2 + \int \frac{n_R(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} d^3r' + V_{xc}(\mathbf{r}) - \sum_I \frac{Z_I}{|\mathbf{r}-\mathbf{R}_I|} \right) \psi_k(\mathbf{r}) \equiv h_0(\mathbf{r}) \psi_k(\mathbf{r}) = \epsilon_k \psi_k(\mathbf{r})$$


Charge density profile of N-Heterocyclic carbenes

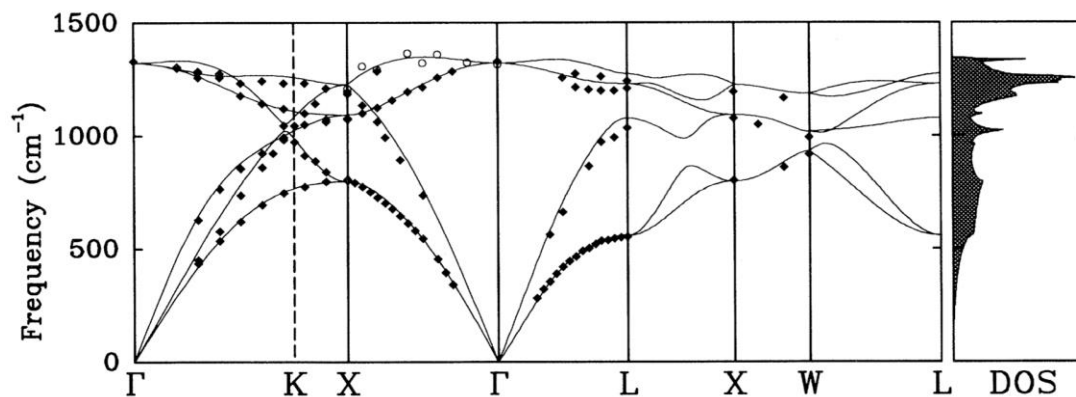


# AB-INITIO CALCULATIONS: Density Functional Theory(2) Crystal Vibrations

STM images



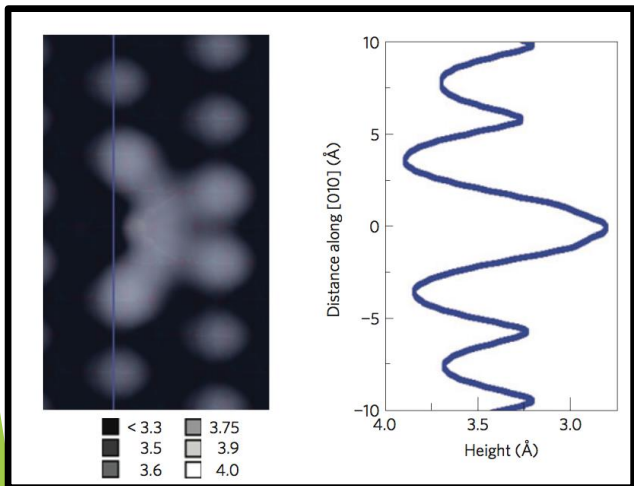
F. Gala et al. J. Phys. Chem. C 2016, 120, 450-456



S. Baroni et al. - Rev. Mod. Phys. 73, 515 (2001)

Phonon Dispersion  
in Diamond

$$\frac{\partial^2 E(\mathbf{R})}{\partial \mathbf{R}_I \partial \mathbf{R}_J} = - \frac{\partial F_I}{\partial \mathbf{R}_J}$$

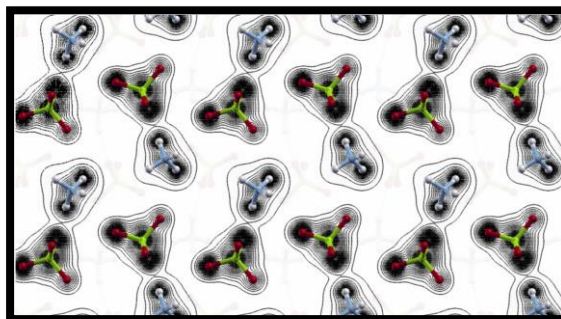


Y. He et al. - Nature Material 8, 585-589 (2009)

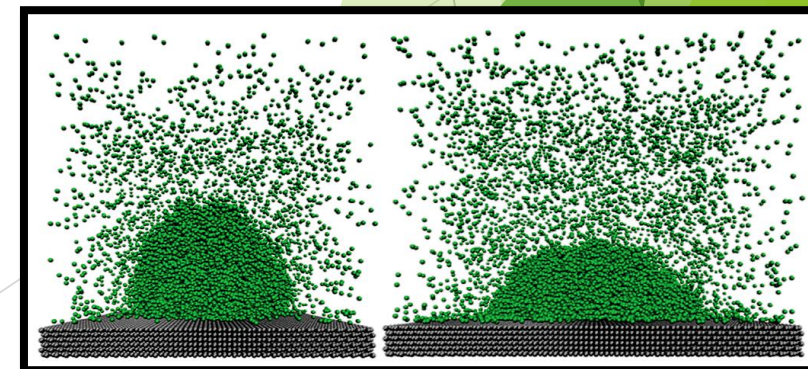
**Ionic Forces (Hellmann-Feynman Theorem):**

$$\mathbf{F}_I = - \frac{\partial E(\mathbf{R})}{\partial \mathbf{R}_I} = - \int n_{\mathbf{R}}(\mathbf{r}) \frac{\partial}{\partial \mathbf{R}_I} \left( - \sum_I \frac{Z_I}{|\mathbf{r} - \mathbf{R}_I|} \right) d^3r - \frac{\partial}{\partial \mathbf{R}_I} \sum_{I \neq J} \frac{Z_I Z_J}{|\mathbf{R}_J - \mathbf{R}_I|}$$

**Electrostatic Potential**

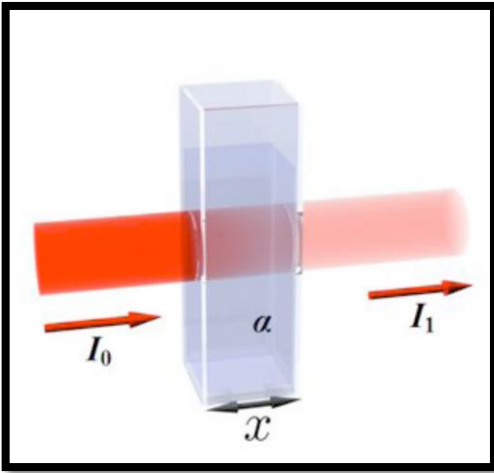


Molecular Dynamics

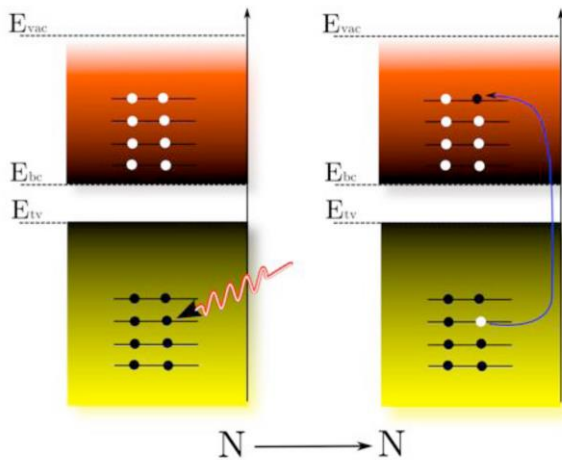




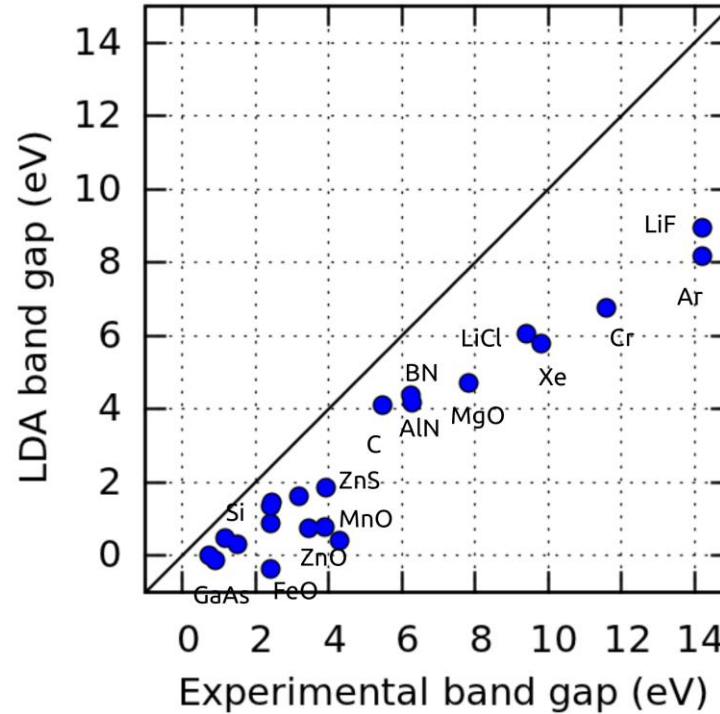
Light Absorption



Beer–Lambert law:  $I_1 = I_0 e^{-\alpha x}$



Beyond DFT(1)



F. Tran et al. – Phys. Rev. Lett. 102, 226401 (2009)

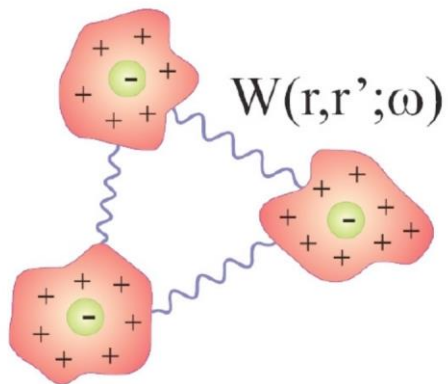
**DFT underestimate experimental band gaps (since  $V_{xc}(r)$  as a function of  $N$  is not a continuous function)**

In absorption (as well as in direct/inverse photoemission) measurements, the excited electron interacts with a hole in the Fermi sea and can not be supposed to be a free electron decoupled from the surrounding.



# GW approximation and Bethe-Salpeter Equations

## Quasi Particle Picture



**W is an effective screened potential**

$$W(\mathbf{r}, \mathbf{r}', \omega) = \int \frac{\epsilon^{-1}(\mathbf{r}, \mathbf{r}'', \omega)}{|\mathbf{r}'' - \mathbf{r}'|} d^3r''$$

**weaker than the bare Coulomb interaction**

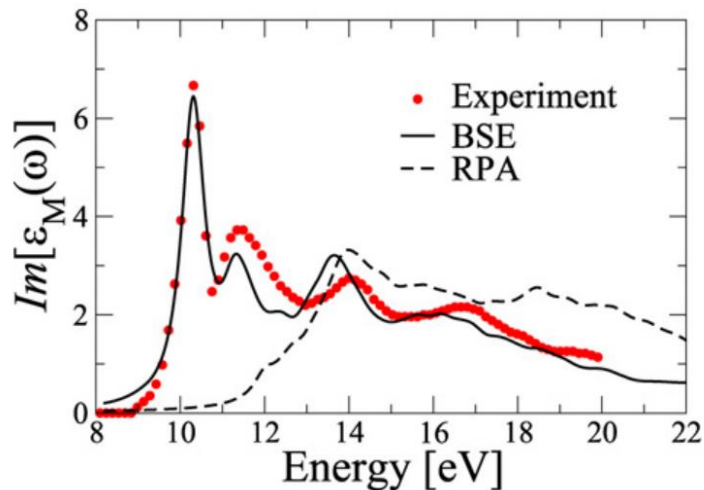
$$G(\mathbf{r}t, \mathbf{r}'t') = -i \frac{\langle \Psi_0 | T \{ \psi(\mathbf{r}t) \psi^\dagger(\mathbf{r}'t') \} | \Psi_0 \rangle}{\langle \Psi_0 | \Psi_0 \rangle}$$

$$[\omega - h_0(\mathbf{r}) - V_{xc}(\mathbf{r})]G(\mathbf{r}, \mathbf{r}') - \int d^3r_1 \Sigma(\mathbf{r}, \mathbf{r}_1; \omega)G(\mathbf{r}_1, \mathbf{r}') = \delta^{(3)}(\mathbf{r} - \mathbf{r}')$$

(Non Local) Self-Energy Term

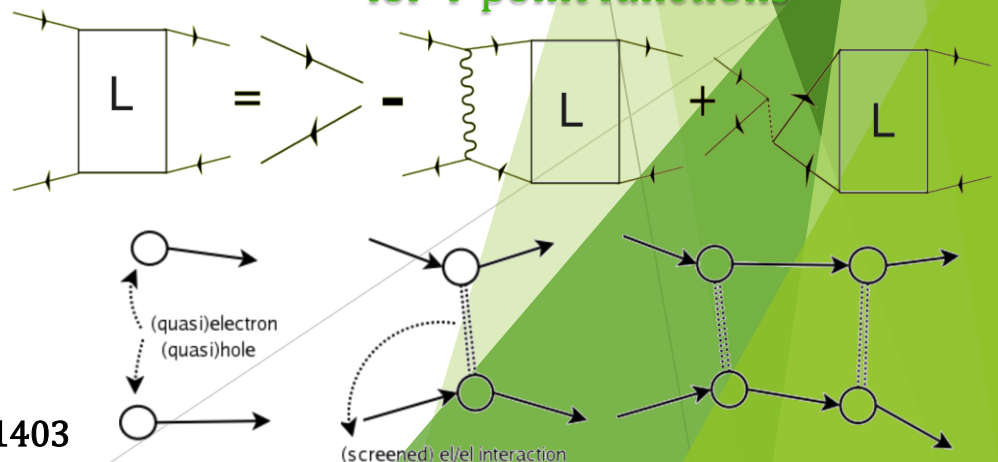


**Excitonic Effects = Electron/Hole interaction**



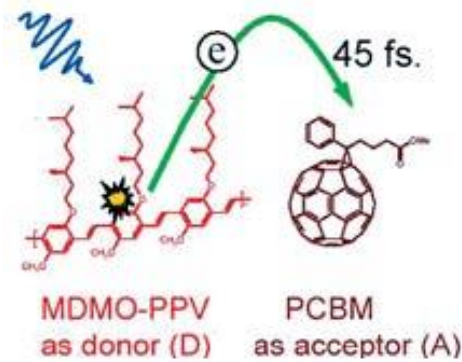
Absorption Spectra of Solid SiO<sub>2</sub>  
from Marini et al. - Comp. Phys. Comm. 180 (2009) 1392-1403

## Bethe-Salpeter Equation for 4-point functions

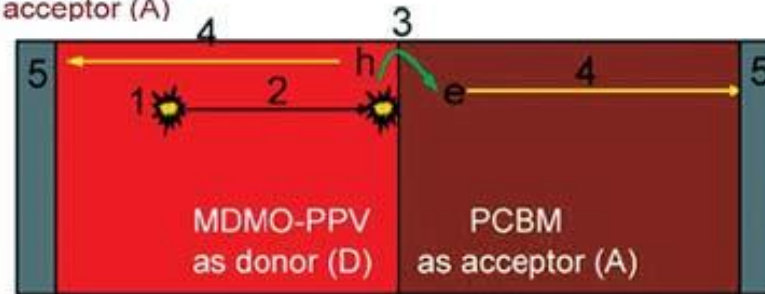




# Bulk Heterojunction (BHJ) Solar Cells



1. Creation of exciton/ excited state/ e-h pair
2. Diffusion of exciton towards interface
3. Charge transfer
4. Charge transport in two different phases
5. Collection of charges at electrodes



*«The initial discovery of ultrafast electron transfer occurred in late 1992. It was a discovery based purely on curiosity. At that time, we had been working on the optical properties of semiconducting polymers for many years. Then, the fullerenes were discovered[...]. During a random discussion in my office, we speculated on what would happen if we mixed these two novel materials. We made several speculative guesses, but decided to do some initial experiments even though the idea was not yet well formed in our minds. We obtained the now famous soluble fullerene derivative, PCBM, from Fred Wudl and the story began to unfold.»*

*Alan J. Heeger*

(Nobel Prize in Chemistry 2000)

Heeger A. J. - Adv. Mater. 2014, 26, 10-28

KITCHEN SCIENCE

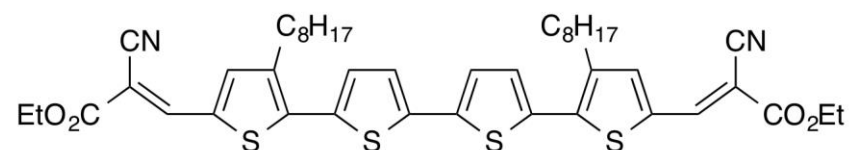
PCBM : Phenyl-C61-butyric acid methyl ester

MDMO-PPV: Poly[2-methoxy-5-(3',7'-dimethyloctyloxy)-1,4-phenylenevinylene]



# BT2N as donor material in BHJ: Experimental Evidences

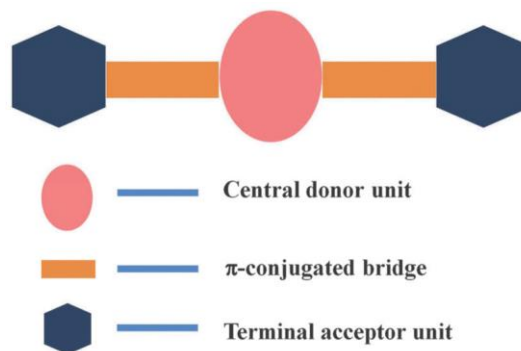
BT2N Molecular Formula :



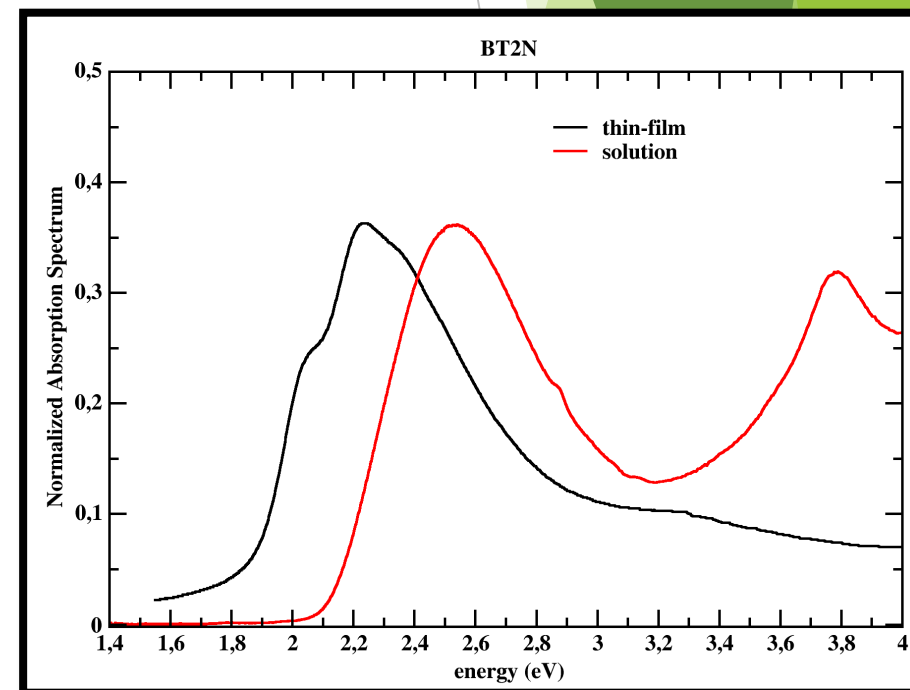
Oligothiophene derivatives exposed to ultraviolet light at 254 nm (left) and 365 nm (right)



**Acceptor-Donor-Acceptor (A-D-A) Structure**



from Ni W. et al. - Chem. Commun.,  
2015, 51, 4936-4950

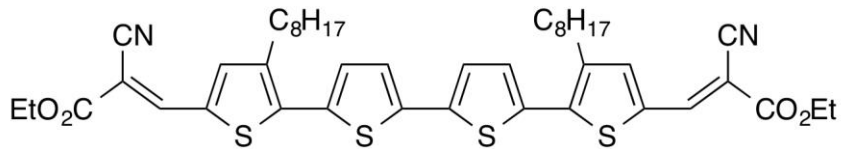


BT2N absorption spectrum

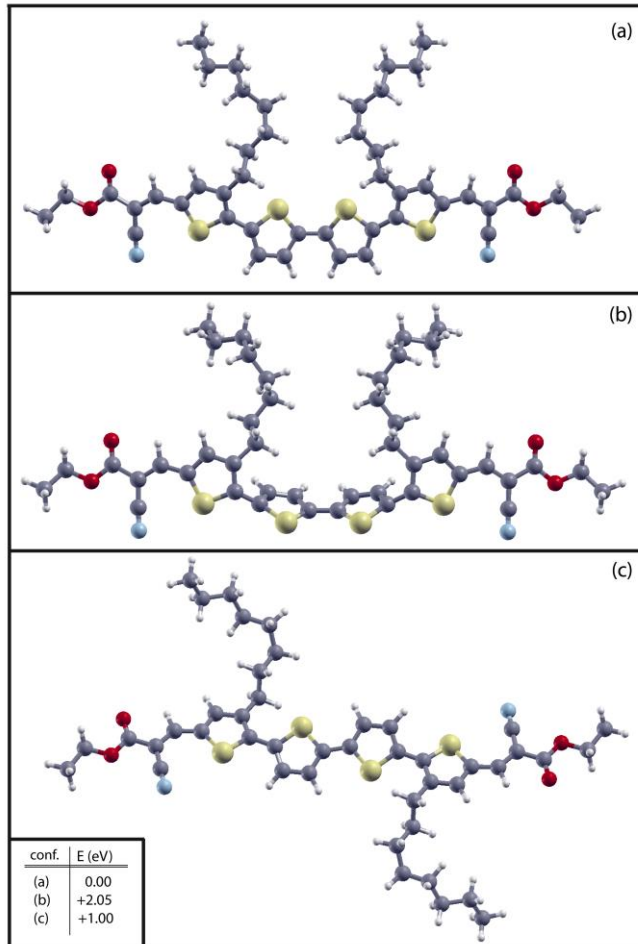


# Modelling oligothiophene small-molecules from first principles

BT2N Molecular Formula :



The bare chemical formula does not give any insight about the relaxed geometry of the molecule



Starting trial configurations have been chosen according to:

- Symmetry Considerations
- Hindrance minimization

IONIC RELAXATION

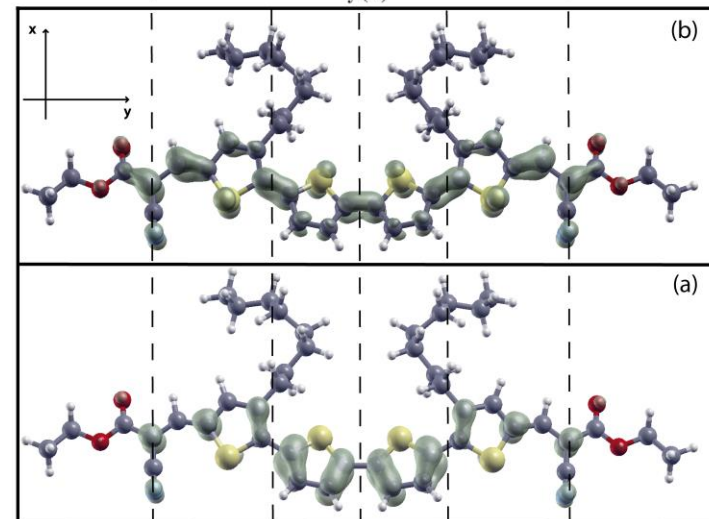
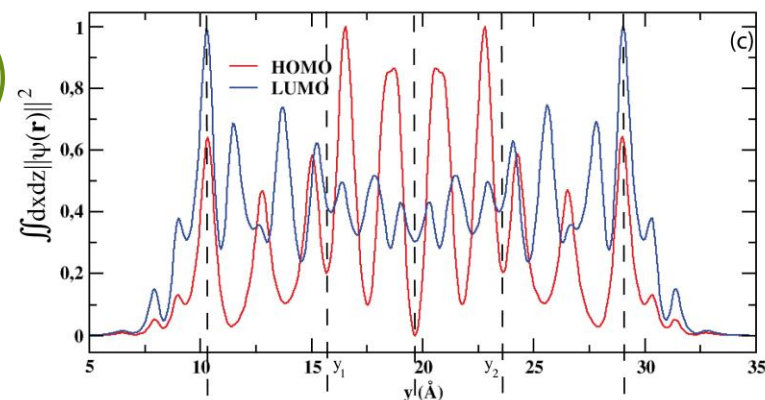
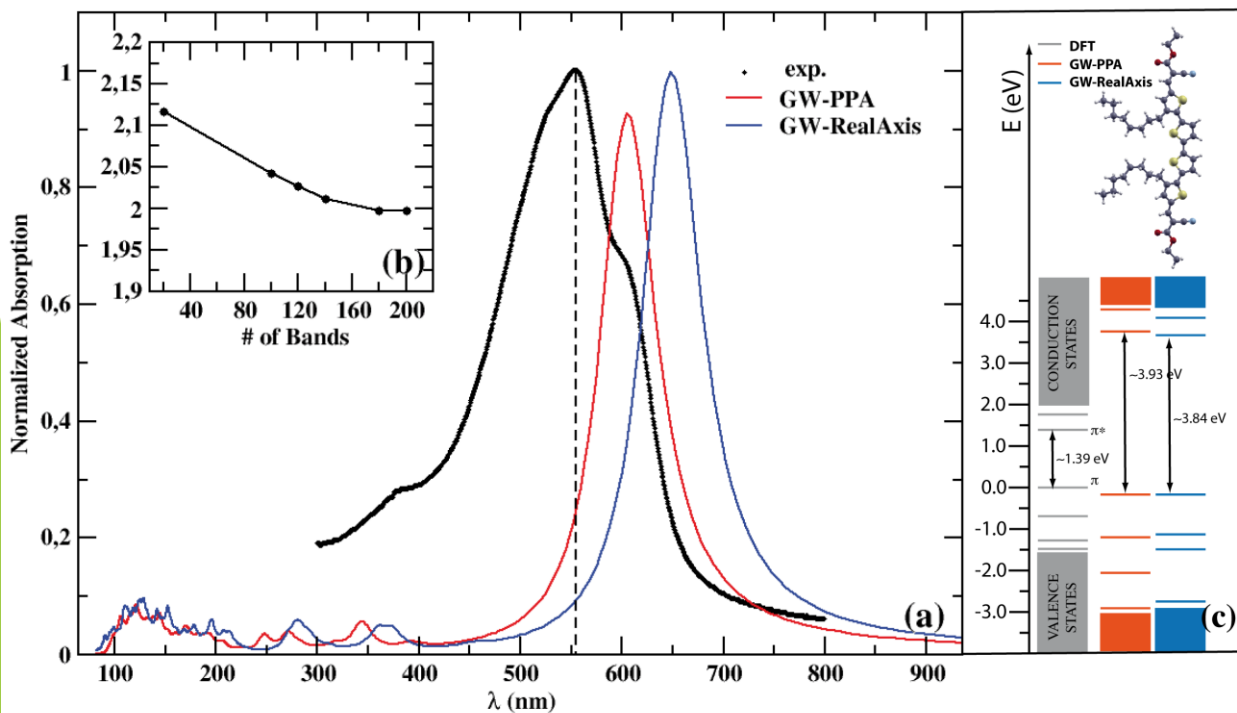


# BT2N Electronic Properties: Gas Phase

Name	$\epsilon_{\text{HOMO}}$ (eV)		$\epsilon_{\text{LUMO}}$ (eV)		$\epsilon_{\text{gap}}$ (eV)		Structure
	DFT-PBE	exp.	DFT-PBE	exp.	DFT-PBE	exp.	
BT2N	-4.96 (-4.56)	-5.49	-3.57 (-3.27)	-3.47	1.39 (1.30)	2.02	

$P_{\text{HOMO}}^{\text{HOMO}} \sim 0.53$   
 $P_{\text{LUMO}}^{\text{LUMO}} \sim 0.31$

Isosurface plots for the calculated HOMO and LUMO orbitals ( (a) and (b), respectively), together with their normalized  $xz$  average values (c).

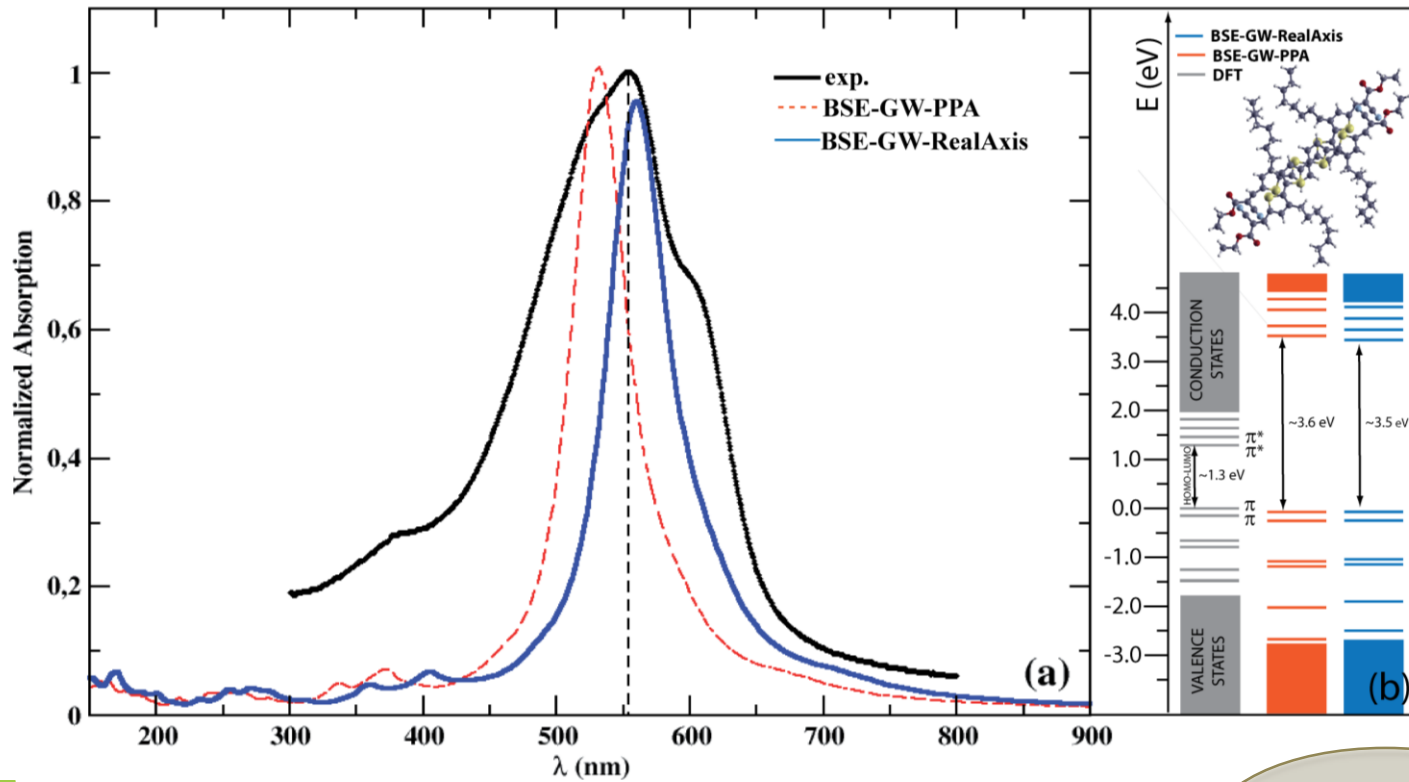


**A-D-A Structure ??**



# BT2N Electronic Properties: Solid State Phase

$\pi$  conjugation between BT2N molecules



The absorption properties of small oligothiophene molecules are tightly related to the way they are arranged in the matrix of organic solar cell device.

Clausius-Mossotti relation:  $\alpha_{\parallel} = \frac{3\Omega \epsilon_{\parallel} - 1}{4\pi \epsilon_{\parallel} + 2}$

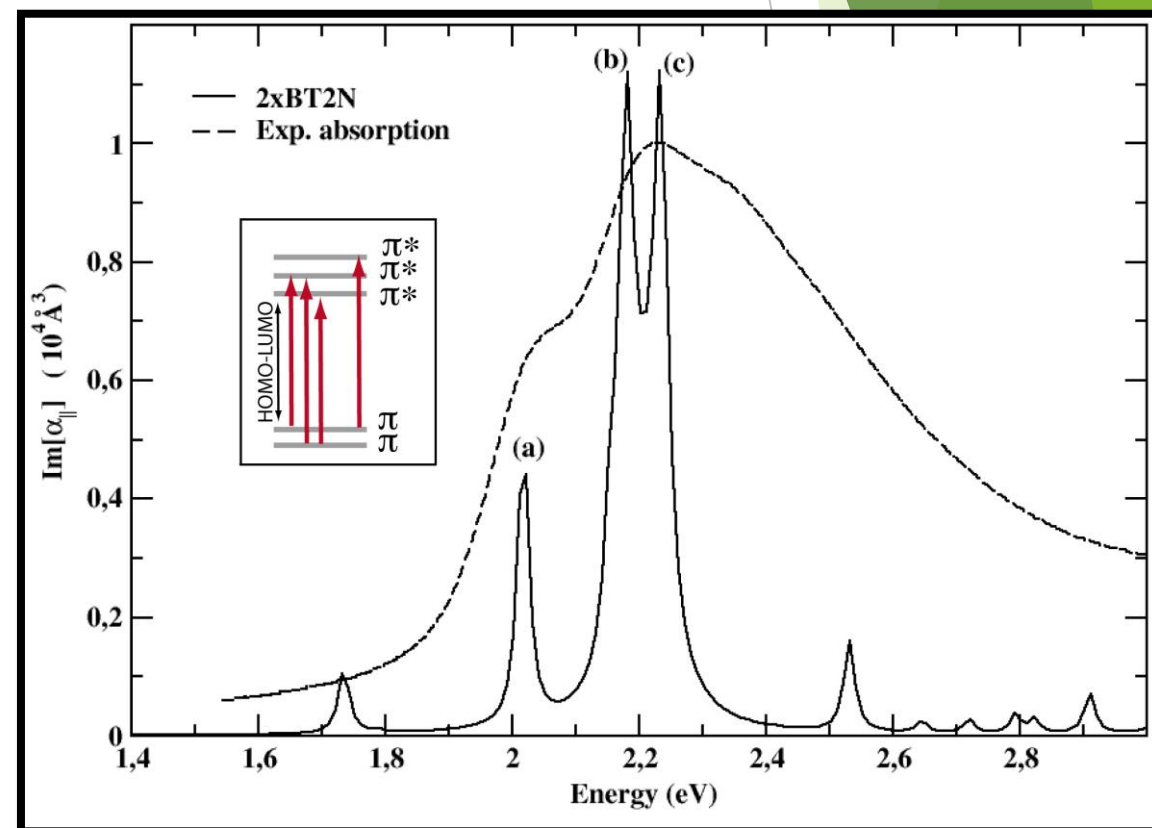
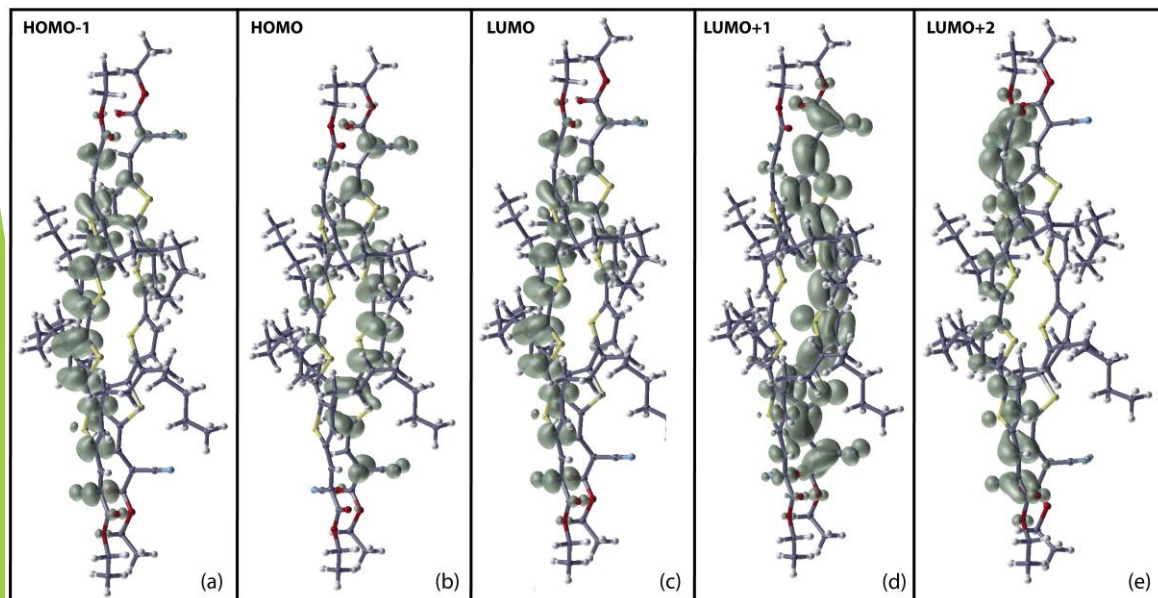
$$\epsilon_M(\omega) = 1 - \lim_{\mathbf{q} \rightarrow 0} V(\mathbf{q}) \lim_{\eta \rightarrow 0^+} \sum_{\lambda\lambda'} \sum_{n_1 n_2} \langle n_1 | e^{-i\mathbf{q} \cdot \mathbf{r}} | n_2 \rangle \frac{A_{n_1 n_2}^{\lambda}}{\omega - E_{\lambda} + i\eta} \times S_{\lambda\lambda'}^{-1} \sum_{n_3 n_4} (f_{n_3} - f_{n_4}) \langle n_4 | e^{i\mathbf{q} \cdot \mathbf{r}'} | n_3 \rangle (A_{n_3 n_4}^{\lambda'})^*$$

# BT2N Excitonic Properties

experimental  
band gap!

Peak	E (eV)	eh pairs	Weight $A_{nn'}^\lambda$
(a)	2.02	HOMO-1 → LUMO+1	0.61
		HOMO → LUMO+1	0.25
		HOMO-1 → LUMO	0.12
(b)	2.18	HOMO → LUMO + 2	0.87
(c)	2.23	HOMO-1 → LUMO	0.30
		HOMO-1 → LUMO+1	0.30
		HOMO → LUMO+1	0.25

$$\Phi^\lambda(\mathbf{r}_e, \mathbf{r}_h) = \sum_{nn'} A_{nn'}^\lambda \phi_n(\mathbf{r}_e) \phi_{n'}^*(\mathbf{r}_h)$$







## Future Developments

- Evaluation of Exciton Lifetime/Diffusion Length in small molecules

$$L = (D\tau)^{\frac{1}{2}} \propto \tau^{\frac{1}{2}}$$

- Inspect the role of ionic degrees of freedom (phonons) in the exciton formation
- Evaluate the charge transfer rate at the interface with PCBM

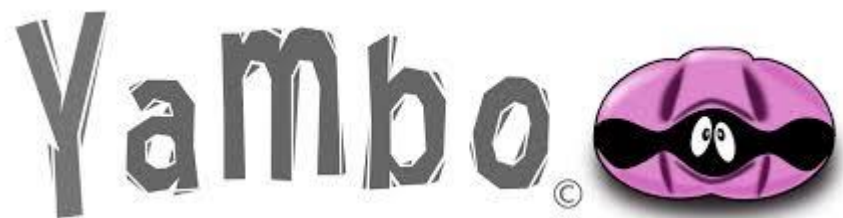


**SAPIENZA**  
UNIVERSITÀ DI ROMA

**Nano** Rome, 20-23 September  
**2016 Innovation**  
Conference & Exhibition

# Thanks To the Audience

Calculations performed with:



Computing resources for this works have been provided by



CRESCO/ENEAGRID HPC infrastructure is funded by ENEA, see <http://www.cresco.enea.it> for information.



## ..and to the Co-Authors



**Dr. Leonardo Mattiello**



**Dr. Francesca Brunetti**



**Dr. Giuseppe Zollo**